

## 5.1 Trig Identities

Simplify the following.

1.  $\sec^2 \theta (1 - \sin^2 \theta)$

~~$\sec^2 \theta - \frac{\sin^2 \theta}{\cos^2 \theta} =$~~   
 $\sec^2 \theta - \tan^2 \theta = 1$

5.  $\tan^2 x - \sec^2 x$

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2.  $\sin x \cot x$

~~$\sin x \frac{\cos x}{\sin x} =$~~   
 $\cos x$

6.  $\sec x \cot x \sin x$

~~$\frac{\cos x \sin x}{\cos x \sin x} = 1$~~

3.  $(\sin \theta - 1)(\sin \theta + 1)$

~~$\sin^2 x - 1 =$~~   
 $-\cos^2 x$

4.  $1 + \tan^2 \theta$

~~$\sec^2 \theta$~~

8.  $\csc^2 x (1 - \cos^2 x)$

~~$\csc^2 x \cdot \sin^2 x = 1$~~

9.  $\frac{1}{\sin^2 A} - \frac{1}{\tan^2 A}$

~~$\frac{\tan^2 A}{\sin^2 A} / \frac{\sin^2 A}{\sin^2 A} =$~~

~~$\csc^2 A - \cot^2 A = 1$~~

10.  $1 - \frac{\sin^2 A}{\tan^2 A}$

~~$1 - \frac{\sin^2 A \cot^2 A}{\sin^2 A \cdot \cos^2 A} =$~~   
 $1 - \frac{\sin^2 A \cdot \cos^2 A}{\sin^2 A} =$

11.  $\frac{1}{\cos^2 A} - \frac{1}{\cot^2 A}$

~~$\sec^2 A - \tan^2 A = 1$~~

12.  $\frac{\sin^2 a}{1 + \cos a}$

~~$\frac{1 - \cos^2 a}{1 + \cos a} =$~~   
 $1 - \cos a$

13.  $\cos x (\sec x - \cos x)$

~~$1 - \cos^2 x =$~~   
 $\sin^2 x$

14.  $\cos^2 A (\sec^2 A - 1)$

~~$1 - \cos^2 A =$~~   
 $\sin^2 A$

15.  $(\sec B - \tan B)(\sec B + \tan B)$

~~$\sec^2 B - \tan^2 B = 1$~~

16.  $\frac{\sin x \cos x}{1 - \cos^2 x}$

~~$\frac{\sin x \cos x}{\sin^2 x} =$~~   
 $\frac{\cos x}{\sin x} = \cot x$

17.  $\frac{\tan^2 x}{\sec x + 1} + 1$

~~$\frac{\sec^2 x - 1}{\sec x + 1} + 1 =$~~   
 $\frac{\sec x - 1 + 1}{\sec x} =$

18.  $\frac{\sin^2 x}{\cos x} + \cos x$

~~$\frac{\sin^2 x + \cos^2 x}{\cos x} = \sec x$~~

19.  $(\sec^2 x - 1)(\csc^2 x - 1)$

~~$\tan^2 x \cdot \cot^2 x = 1$~~

20.  $\tan^2 \theta - \sec^2 \theta = 1$

21.  $\tan \theta \csc \theta$

~~$\frac{\sin x}{\cos x} \cdot \frac{1}{\sin x} =$~~   
 $\sec x$

22.  $(1 + \cot^2 x)(1 - \cos^2 x)$

~~$\csc^2 x \cdot \sin^2 x = 1$~~

23.  $(1 - \sin^2 \theta)(1 + \tan^2 \theta)$

~~$\cos^2 \theta \cdot \sec^2 \theta = 1$~~

24.  $\sec \theta - (\tan \theta \sin \theta)$

~~$\frac{1}{\cos \theta} - \frac{\sin^2 \theta}{\cos \theta}$~~   
 $\frac{\cos^2 \theta}{\cos \theta} =$   
 $\cos \theta$

25.  $\cos \theta (\sec \theta - \cos \theta)$

~~$1 - \cos^2 \theta$~~   
 $\sin^2 \theta$

26.  $\csc^2 x (1 - \cos^2 x)$

~~$\csc^2 x \cdot \sin^2 x = 1$~~